Basic Electrical Engineering

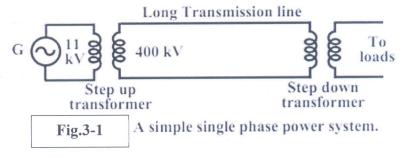
Single Phase Transformer

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What is a Transformer?

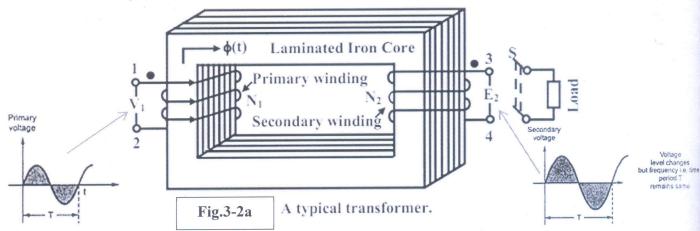
A transformer is a static piece of equipment used either for raising or lowering the voltage of an AC supply with a corresponding decrease or increase in current.

The use of transformers in transmission system is shown in the Figure below.

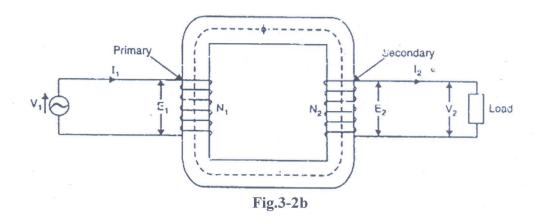


Principle of Operation

A transformer in its simplest form will consist of a rectangular laminated magnetic structure on which two coils of different number of turns are wound as shown in Figure 3.2a.



The winding to which AC voltage is impressed is called *the primary* of the transformer and the winding across which the load is connected is called *the secondary* of the transformer.



Depending upon the number of turns of the primary (N_1) and secondary (N_2) , an alternating emf (E_2) is induced in the secondary. This induced emf (E_2) in the secondary causes a secondary current I_2 . Consequently, terminal voltage V_2 will appear across the load. If $V_2 > V_1$, it is called a *step up-transformer*. On the other hand, if $V_2 < V_1$, it is called a *step-down transformer*.

When an alternating voltage V_1 is applied to the primary, an alternating flux Φ is set up in the core. This alternating flux links both the windings and induces emfs E1 and E2 in them according to *Faraday's laws of electromagnetic induction*. The emf E1 is termed as primary emf and emf E2 is termed as Secondary emf.

Clearly,
$$E_1 = -N_1 \frac{d\phi}{dt}$$

and $E_2 = -N_2 \frac{d\phi}{dt}$
 $\therefore \frac{E_2}{E_1} = \frac{N_2}{N_1}$

Note that magnitudes of E_2 and E_1 depend upon the number of turns on the secondary and primary respectively. If $N_2 > N_1$, then $E_2 > E_1$ (or $V_2 > V_1$) and we get a step-up transformer. On the other hand, if $N_2 < N_1$, then $E_2 < E_1$ (or $V_2 < V_1$) and we get a step-down transformer. If load is connected across the secondary winding, the secondary e.m.f. E_2 will cause a current I_2 to flow through the load. Thus, a transformer enables us to transfer a.c. power from one circuit to another with a change in voltage level.

The following points may be noted carefully:

- (i) The transformer action is based on the laws of *electromagnetic* induction.
- (ii) There is no electrical connection between the primary and secondary.
- (iii) There is no change in frequency i.e., output power has the same frequency as the input power.

Can DC Supply be used for Transformers?

The DC supply cannot be used for the transformers. This is because the transformer works on the principle of mutual induction, for which current in one coil must change uniformly. If DC supply is given, the current will not change due to constant supply and transformer will not work

There can be saturation of the core due to which transformer draws very large current from the supply when connected to DC.

Thus DC supply should not be connected to the transformers.

Construction

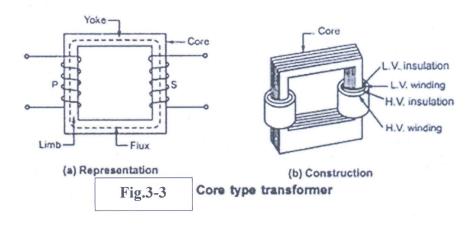
We usually design a power transformer so that it approaches the characteristics of an ideal transformer. To achieve this, following design features are incorporated:

- (i) The core is made of silicon steel which has low hysteresis loss and high permeability. Further, core is laminated in order to reduce eddy current loss. These features considerably reduce the iron losses and the no-load current.
- (ii) Instead of placing primary on one limb and secondary on the other, it is a usual practice to wind one-half of each winding on one limb. This ensures tight coupling between the two windings. Consequently, leakage flux is considerably reduced.

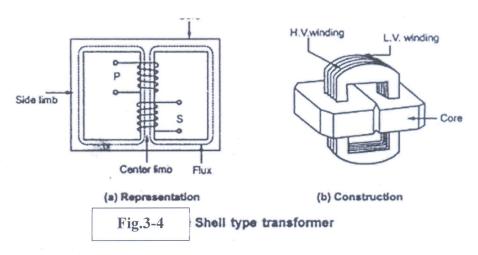
(iii) The winding resistances are minimized to reduce Copper loss and resulting rise in temperature and to ensure high efficiency.

Transformers are of two types: (i) core-type transformer (see Fig.3-3) and (ii) shell-type transformer (see Fig.3-4).

Core-Type Transformer: In a core-type transformer, half of the primary winding and half of the secondary winding are placed round each limb to reduce the leakage flux.



Shell-Type Transformer: This method of construction involves the use of a double magnetic circuit. Both the windings are placed round the central limb to ensure a low-reluctance flux path.



Comparison of Core and Shell Type Transforms

Core Type	Shell Type
The winding encircles the core.	The core encircles most part of the winding
It has single magnetic circuit	It has double magnetic circuit
The core has two limbs	The core has three limbs
The cylindrical coils are used.	The multilayer disc or sandwich type coils are used.
The winding are uniformly distributed on two limbs hence natural cooling is effective	The natural cooling does not exist as the windings are surrounded by the core.
Preferred for low voltage transformers.	Preferred for high voltage transformers.

Cooling of Transformers

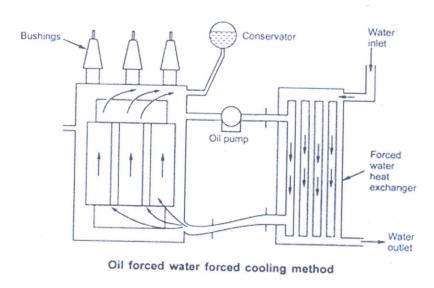
When transformer supplies a load, two types of losses occur inside the transformer. The iron losses occur in the core while copper losses occur in the windings. The power lost due to these losses appears in the form of heat. This heat increases the temperature of the transformer. To keep the temperature rise of the transformer within limits, a suitable coolant and cooling method is necessary.

The various cooling methods are designated witch depended upon:

A: cooling medium used and B: type of circulation employed.

The various coolant used such as Air, Gas, Mineral oil, and water.

One of cooling method system is shown in figure below which is called *Oil Forced Water Forced cooling system*;



EMF Equation of a Transformer

Consider that an alternating voltage V_1 of frequency f is applied to the primary as shown in Fig. 3-2b. The sinusoidal flux Φ produced by the primary can be represented as:

$$\phi = \phi_m \sin \omega t$$

The instantaneous e.m.f. e1 induced in the primary is

$$e_1 = -N_1 \frac{d\phi}{dt} = -N_1 \frac{d}{dt} (\phi_m \sin \omega t)$$

$$= -\omega N_1 \phi_m \cos \omega t = -2\pi f N_1 \phi_m \cos \omega t$$

$$= 2\pi f N_1 \phi_m \sin(\omega t - 90^\circ)$$
(i)

It is clear from the above equation that maximum value of induced e.m.f. in the primary is

$$E_{ml} = 2\pi f N_1 \phi_m$$

The r.m.s. value E^ of the primary e.m.f. is

$$E_1 = \frac{E_{m1}}{\sqrt{2}} = \frac{2\pi f N_1 \phi_m}{\sqrt{2}}$$

O

$$E_1 = 4.44 \text{ f } N_1 \phi_m$$

Similarly

$$E_2 = 4.44 \text{ f N}_2 \phi_m$$

In an ideal transformer, $E_1 = V_1$ and $E_2 = V_2$.

Note. It is clear from exp. (i) above that e.m.f. E_1 induced in the primary lags behind the flux ϕ by 90°. Likewise, e.m.f. E_2 induced in the secondary lags behind flux ϕ by 90°.

Voltage Transformation Ratio (K)

From the above equations of induced emf, we have,

$$\frac{E_2}{E_1} = \frac{N_2}{N_1} = K$$

The constant K is called voltage transformation ratio. Thus if K = 5 (i.e.

N2/N1 = 5), then E2 = 5 E1.

Concept of Ideal Transformer

A transformer is said to be ideal if it satisfies following properties:

- i) It has no losses.
- ii) Its windings have zero resistance.
- iii) Leakage flux is zero i.e. 100 % flux produced by primary links with the secondary.
- iv) Permeabitity of core is so high that negilgible current is required to establish the flux in it.

NOTE:

For an ideal transformer, the primary applied voltage V1 is same as the primary induced emf E1 as there are no voltage drops.

$$\therefore \frac{E_2}{E_1} = \frac{V_2}{V_1} = \frac{N_2}{N_1} = K$$

(ii) there are no losses. Therefore, volt-amperes input to the primary are equal to the output volt-amperes i.e.

$$V_1 I_1 = V_2 I_2$$

or
$$\frac{I_2}{I_1} = \frac{V_1}{V_2} = \frac{1}{K}$$

Hence, currents are in the inverse ratio of voltage transformation ratio. This simply means that if we raise the voltage, there is a corresponding decrease of current.

Volt-Ampere Rating

Transformer rating is specified as the product of voltage and current and called *VA rating*.

kVA rating of a =
$$\frac{V_1 I_1}{1000}$$
 = $\frac{V_2 I_2}{1000}$

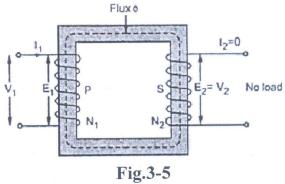
The full load primaty and secondary currents which indicate the safe maximum values of currents which transformer windings can carry can be given as:

$$I_1$$
 full load = $\frac{\text{kVA rating} \times 1000}{V_1}$... (1000 to convert kVA to VA)
 I_2 full load = $\frac{\text{kVA rating} \times 1000}{V_2}$

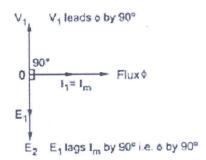
Ideal Transformer on No Load

Consider an ideal transformer in Fig. 3-5. For no load I_2 =0. I_1 is just necessary to produce flux in the core, which is called *magnetising* current denoted as I_m . I_m is very small and lags V_1 by 90^0 as the winding is purely inductive.

According to Lenz's law, the induced e.m.f opposes the cause producing it which is supply voltage V₁. Hence E₁ and E₂ are in antiphase with V₁ but equal in magnitude and E_1 and E_2 are in phase.



This can be illustrated in the phase diagram as shown below:

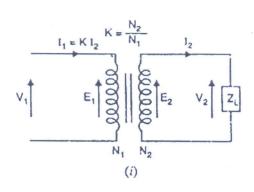


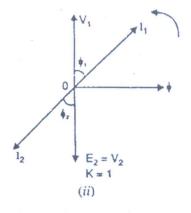
Phasor diagram for ideal transformer on no load

Ideal Transformer on Load

Let us connect a load Z_{L} across the secondary of an ideal transformer as shown in Figure below:

The secondary emf E2 will cause a current I_2 to flow through the load:





$$I_2 = \frac{E_2}{Z_L} = \frac{V_2}{Z_L}$$

The angle at which I_2 leads or lags V_2 (or E_2) depends upon the resistance and reactance of the load. In the present case, we have considered inductive load so that current I_2 lags behind V_2 (or E_2) by ϕ_2 .

The secondary current I_2 sets up an m.m.f. N_2I_2 which produces a flux in the opposite direction to the flux ϕ originally set up in the primary by the magnetizing current. This will change the flux in the core from the original value. However, the flux in the core should not change from the original value.

Thus when a transformer is loaded and carries a secondary current I_2 , then a current I_1 , (= K I_2) must flow in the primary to maintain the m.m.f. balance. In other words, the primary must draw enough current to neutralize the demagnetizing effect of secondary current so that mutual flux ϕ remains constant. Thus as the secondary current increases, the primary current I_1 (= K I_2) increases in unison and keeps the mutual flux ϕ constant. The power input, therefore, automatically increases with the output. For example if K = 2 and I_2 = 2A, then primary will draw a current I_1 = K I_2 = 2 × 2 = 4A. If secondary current is increased to 4A, then primary current will become I_1 = K I_2 = 2 × 4 = 8A.

The Phasor diagram for the ideal transformer on load is shown in Figure (ii) above.

The secondary current I_2 lags behind V_2 (or E_2) by Φ_2 . It causes a primary current $I_1 = KI_2 = I2$ (for K=1) which is in antiphase with it.

(i)
$$\phi_1 = \phi_2$$

or
$$\cos \phi_1 = \cos \phi_2$$

Thus, power factor on the primary side is equal to the power factor on the secondary side.

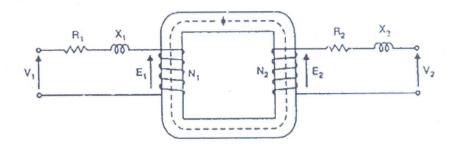
(ii) Since there are no losses in an ideal transformer, input primary power is equal to the secondary output power i.e.,

$$V_1 I_1 \cos \phi_1 = V_2 I_2 \cos \phi_2$$

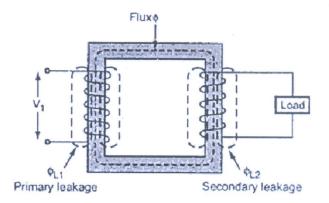
Practical Transformer

A practical transformer differs from the ideal transformer in many respects. The practical transformer has (i) *iron losses* (ii) *winding resistances* and (iii) *magnetic leakage*, giving rise to leakage reactance.

- (i) Iron losses. Since the iron core is subjected to alternating flux, there occurs eddy current and hysteresis loss in it.
- (ii) Winding resistances. Since the windings consist of copper conductors, it immediately follows that both primary and secondary will have winding resistance. The primary resistance R1 and secondary resistance R2 act in series with the respective windings as shown below:

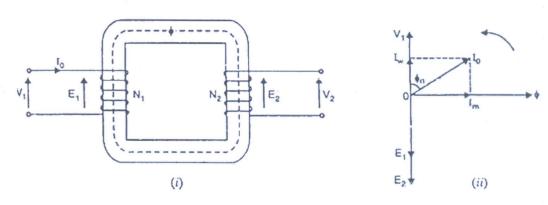


(iii) Leakage reactance. Both primary and secondary currents produce flux. The flux Φ which links both the windings is the useful flux However, primary current would produce some flux Φ which would not link the secondary winding and is called mutual flux (for more information review Lecture Note 2) (See Fig. below).



Practical Transformer on No Load

Consider the figure below:



The primary will draw a small current I_0 to supply (i) the iron losses and (ii) a very small amount of copper loss in the primary. Hence the primary no load current I_0 is not 90° behind the applied voltage V_1 but lags it by an angle $\Phi_0 < 90^\circ$ as shown in the phasor diagram.

The no-load primary current I_0 can be resolved into two rectangular components:

(i) The component I_W in phase with the applied voltage V_1 . This is known as active or working or iron loss component and supplies the iron loss and a very small primary copper loss.

$$I_{W} = I_{0} \cos \phi_{0}$$

The component I_m lagging behind V_1 by 90° and is known as magnetizing component. It is this component which produces the mutual flux ϕ in the core.

$$I_{\rm m} = I_0 \sin \phi_0$$

Clearly, Io is phasor sum of Im and IW,

$$\therefore \quad I_0 = \sqrt{I_m^2 + I_W^2}$$

No load p.f.,
$$\cos \phi_0 = \frac{I_W}{I_0}$$

It is emphasized here that no load primary copper loss (i.e. $I_0^2 R_1$) is very small and may be neglected. Therefore, the no load primary input power is practically equal to the iron loss in the transformer i.e.,

No load input power, $W_0 = Iron loss$

Note. At no load, there is no current in the secondary so that $V_2 = E_2$. On the primary side, the drops in R_1 and X_1 , due to I_0 are also very small because of the smallness of I_0 . Hence, we can say that at no load, $V_1 = E_1$.

Practical Transformer on Load

We shall consider two cases (i) when such a transformer is assumed to have no winding resistance and leakage flux (ii) when the transformer has winding resistance and leakage flux.

No winding resistance and leakage flux

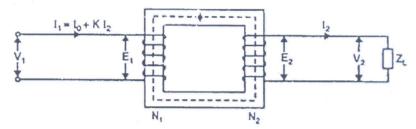


Fig. above shows a practical transformer with the assumption that resistances and leakage reactances of the windings are negligible. With this assumption, $V_2 = E_2$ and $V_1 = E_1$.

Let us take the usual case of inductive load which causes the I_2 to lag V_2 by Φ_2 . The total primary current I_1 must meet two requirements:

- (a) It must supply the no-load current I₀ to meet the iron losses in the transformer and to provide flux in the core.
- (b) It must supply a current I'₀ to counteract the demagnetizing effect of secondary currently I₂. The magnitude of I'₂ will be such that:

$$N_1 I'_2 = N_2 I_2$$

or
$$I'_2 = \frac{N_2}{N_1} I_2 = KI_2$$

The total primary current I_1 is the phasor sum of I'_2 and I_0 i.e.,

$$I_1 = I'_2 + I_0$$

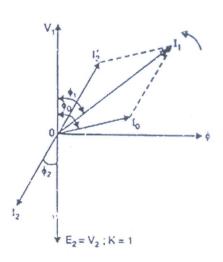
where $I'_2 =$

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$$I'_2 = -KI_2$$

Note that Γ_2 is 180° out of phase with I_2 .

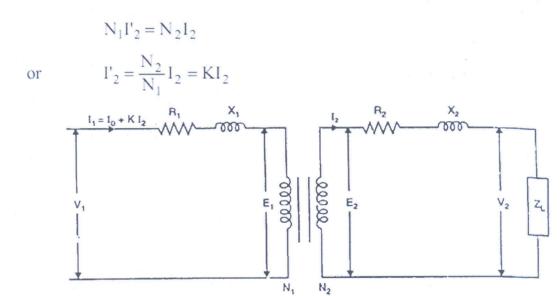
Phasor Diagram: Both E_1 and E_2 lag behind the mutual flux f by 90°. The current I'_2 represents the primary current to neutralize the demagnetizing effect of secondary current I_2 . Now $I'_2 = K I_2$ and is antiphase with I_2 . I_0 is the no-load current of the transformer. The phasor sum of I'_2 and I_0 gives the total primary current I_1 . Note that in drawing the phasor diagram, the value of K is assumed to be unity so that primary phasors are equal to secondary phasors.



Transformer with resistance and leakage reactance

The total primary current I₁ must meet **two requirements**:

- (a) It must supply the no-load current I_0 to meet the iron losses in the transformer and to provide flux in the core.
- (b) It must supply a current I'₂ to counteract the demagnetizing effect of secondary current I₂. The magnitude of I'₂ will be such that:



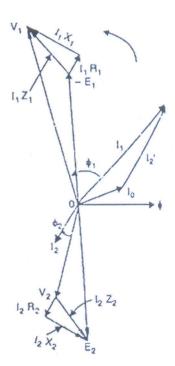
The total primary current I_1 will be the phasor sum of I'_2 and I_0 i.e.,

$$\begin{split} I_1 &= I'_2 + I_0 & \text{where} & I'_2 = -KI_2 \\ V_1 &= -E_1 + I_1(R_1 + jX_1) & \text{where} & I_1 = I_0 + (-KI_2) \\ &= -E_1 + I_1Z_1 \\ V_2 &= E_2 - I_2(R_2 + jX_2) \\ &= E_2 - I_2Z_2 \end{split}$$

Phasor Diagram:

Note that counter emf that opposes the applied voltage V_1 is $-E_1$. Therefore, if we add I_1R_1 (in phase with I_1) and $I_1 X_1$ (90° ahead of I_1) to $-E_1$, we get the applied primary voltage V_1 . The phasor E_2 represents the induced emf in the secondary by the mutual flux. The secondary terminal voltage V_2 will be what is left over after subtracting I_2R_2 and I_2X_2 from E_2 .

Load power factor = $\cos \phi_2$ Primary power factor = $\cos \phi_1$ Input power to transformer, $P_1 = V_1I_1 \cos \phi_1$ Output power of transformer, $P_2 = V_2I_2 \cos \phi_2$

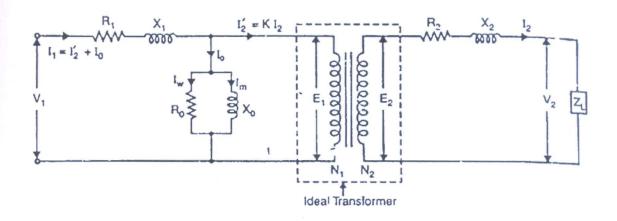


What the Importance of Shifting Impedances?

If we shift all the impedances from one winding to the other, the transformer is eliminated and we get an equivalent electrical circuit. Various voltages and currents can be readily obtained by solving this electrical circuit.

Exact Equivalent Circuit of a Loaded Transformer

The equivalent circuit for the transformer can be represented as shown in the figure.



Where:

R₁: primary winding resistance

R₂: secondary winding resistance

X₁: leakage reactance of primary winding

X₂: leakage reactance of the secondary winding

R_o: represents the core losses (hysteresis and eddy current losses)

X₀: represents magnetising reactance of the core

I_m: magnetizing current (to create magnetic flux in the core)

I_w: active current (required to supply the core losses)

 $I_o = no load primary current$

- NOTE¹: Parallel circuit R_0 X_0 is the no-load equivalent circuit of the transformer or called exciting circuit.
- NOTE²: The equivalent circuit has created two normal electrical circuits separated only by an ideal transformer whose function is to change values according to the equation:

$$\frac{E_2}{E_1} = \frac{N_2}{N_1} = \frac{I'_2}{I_2}$$

■ NOTE³: If Z_L is the external load across the secondary circuit, voltage E_2 induced in the secondary by mutual flux will produce a secondary current I_2 , hence:

$$V_2 = E_2 - I_2(R_2 + j X_2) = E_2 - I_2 Z_2$$

Similarly supply voltage can be given as

$$V_1 = -E_1 + I_1(R_1 + j X_1) = -E_1 + I_1 Z_1$$

- NOTE⁵: When the transformer is loaded to carry the secondary current I₂, the primary current consists of two components:
 - ightharpoonup I₀ to provide magnetizing current and the current required to supply the core losses.
 - \blacktriangleright primary current I'_2 (= K I_2) required to supply the load connected to the secondary

Transformer Tests

The <u>circuit constants</u>, <u>efficiency</u> and <u>voltage regulation</u> of a transformer can be determined by two simple tests:

(i) open-circuit test and (ii) short-circuit test

Open-Circuit Test

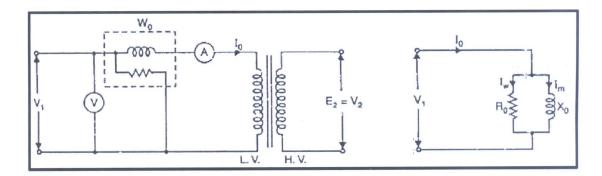
This test is conducted to determine:

- ► The iron losses (or core losses) and
- ightharpoonup Parameters R_0 and X_0 of the transformer.

In this test (see Figure below), the rated voltage is applied to the primary (usually low-voltage winding) while the secondary is left open-circuited.

As the normal rated voltage is applied to the primary, therefore, normal iron losses will occur in the transformer core.

Cu losses in the primary under no-load condition are negligible as compared with iron losses.



For the figure above:

- \circ Iron losses, P_i = Wattmeter reading = W_0
- \circ No load current = Ammeter reading = I_0
- \circ Applied voltage = Voltmeter reading = V_1
- $\circ \quad \text{Input power, } W_0 \ = V_1 \ I_0 \ \text{cos} \varphi_0$

222222222222222222222222222222222

$$\Longrightarrow$$

No-load p.f.,
$$\cos \phi_0 = \frac{W_0}{V_1} I_0$$

$$I_W = I_0 \cos \phi_0; \qquad I_m = I_0 \sin \phi_0$$

$$R_0 = \frac{V_1}{I_W} \quad \text{and} \quad X_0 = \frac{V_1}{I_m}$$

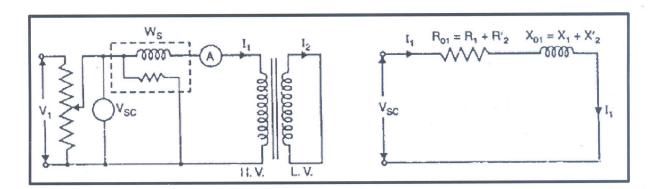
Short-Circuit or Impedance Test

This test is conducted to determine:

- ► Full-load copper losses of the transformer and
- $ightharpoonup R_{01}$ (or R_{02}), X_{01} (or X_{02}).

In this test (see Figure below), the secondary (usually low-voltage winding) is short-circuited by a thick conductor and variable low voltage is applied to the primary.

The low input voltage is gradually raised till at voltage V_{SC} , full-load current I_1 flows in the primary. Then I_2 in the secondary also has full-load value since $I_1/I_2 = N_2/N_1$. Under such conditions, the copper loss in the windings is the same as that on full load.



For the figure above:

- o Full load Cu loss, P_C = Wattmeter reading = W_S
- \circ Applied voltage = Voltmeter reading = V_{SC}
- o F.L. primary current = Ammeter reading = I_1

$$\Longrightarrow$$

$$P_{C} = I_{1}^{2}R_{1} + I_{1}^{2}R'_{2} = I_{1}^{2}R_{01}$$

$$R_{01} = \frac{P_{C}}{I_{1}^{2}}$$

where R₀₁ is the total resistance of transformer referred to primary

Total impedance referred to primary,

$$Z_{01} = \frac{V_{SC}}{I_1}$$

Total leakage reactance referred to primary,

$$X_{01} = \sqrt{Z_{01}^2 - R_{01}^2}$$

Short-circuit pf

$$\cos \phi_2 = \frac{P_C}{V_{SC}I_1}$$

Efficiency from Transformer Tests

The full-load efficiency of the transformer at any pf can be obtained as:

F.L. efficiency,
$$\eta_{F,L.} = \frac{\text{Full - load VA} \times \text{p.f.}}{(\text{Full - load VA} \times \text{p.f.}) + P_i + P_C}$$

where:

P_i = Iron loss can be obtained from open-circuit test

P_c = Copper loss can be obtained from short-circuit test

F.L. = Full Load

Also the efficiency for any load,

Corresponding total losses =
$$P_i + x^2 P_C$$

Corresponding
$$\eta_x = \frac{(xx \text{ Full - load VA}) \times p.f.}{(xx \text{ Full - load VA} \times p.f.) + P_i + x^2 P_C}$$

where xx= Fraction of full-load

NOTE: Iron loss remains the same at all loads.